Likely to stop? Predicting Stopout in Massive Open Online Courses

Colin Taylor Massachusetts Institute of Technology, Cambridge, MA 02139 USA

Kalyan Veeramachaneni Massachusetts Institute of Technology, Cambridge, MA 02139 USA

Una-May O'Reilly

Massachusetts Institute of Technology, Cambridge, MA 02139 USA

Abstract

Understanding why students stopout will help in understanding how students learn in MOOCs. In this report, part of a 3 unit compendium, we describe how we build accurate predictive models of MOOC student stopout. We document a scalable, stopout prediction methodology, end to end, from raw source data to model analysis. We attempted to predict stopout for the Fall 2012 offering of 6.002x. This involved the meticulous and crowd-sourced engineering of over 25 predictive features extracted for thousands of students, the creation of temporal and nontemporal data representations for use in predictive modeling, the derivation of over 10 thousand models with a variety of state-ofthe-art machine learning techniques and the analysis of feature importance by examining over 70000 models. We found that stop out prediction is a tractable problem. Our models achieved an AUC (receiver operating characteristic area-under-the-curve) as high as 0.95 (and generally 0.88) when predicting one week in advance. Even with more difficult prediction problems, such as predicting stop out at the end of the course with only one weeks' data, the models attained AUCs of 0.7.

1. Introduction

Massive Open Online Courses (MOOCs) leverage digital technologies to teach advanced topics at scale. MOOC providers such as edX and Coursera boast hundreds of classes developed by top-tier universities. Renowned professors record their lectures, and when needed, use interactive whiteboards to explain concepts. Recordings are delivered all over the world via web servers at no cost to the learner. Far from compromising the quality of course content, the internet provides a flexible medium for educators to employ new instructional tools. For example, videos enable students to pause, rewind, review difficult concepts and even adjust the speed. In addition, MOOCs allow the learner the flexibility to learn in his or her own time frame. Only in the online medium are short lectures logistically feasible through videos. MOOCs are changing the face of education by providing an alternative to the "one size fits all", learning concept employed by hundreds of universities.

The specific layout of each MOOC varies, but most follow a similar format. Content is sectioned into modules, usually using weeks as intervals. Most MOOCs include online lectures (video segments), lecture questions, homework questions, labs, a forum, a Wiki, and exams. Students advance through the material sequentially, access online resources, submit assignments and participate in peer-to-peer interactions (like the forum).

Not surprisingly, MOOCs have attracted the attention of online learners all over the world. The platforms boast impressive numbers of registrants and individuals who complete online course work. For example, MITx offered its first course 6.002x: Circuits and Electronics in the Fall of 2012. 6.002x had 154,763 regis-

COLIN T@MIT.EDU

KALYAN@CSAIL.MIT.EDU

UNAMAY@CSAIL.MIT.EDU

trants. Of those, 69,221 students looked at the first problem set, and 26,349 earned at least one point. 9,318 students passed the midterm and 5,800 students got a passing score on the final exam. Finally, after completing 15 weeks of study, 7,157 registrants earned the first certificate awarded by MITx, showing they had successfully completed 6.002x. For perspective, approximately 100 students take the same course each year at MIT. It would have taken over 70 years of oncampus education to grant the same number of 6.002x certificates that were earned in a single year online.

While the completion rates are impressive when compared to in-class capacity, they are still low relative to the number of people who registered, completed certain parts of the course or spent a considerable amount of time on the course. To illustrate, in the above scenario approximately 17% attempted and got at least one point on the first problem set. The percentage of students who passed the midterm drops to just 6%, and certificate earners dwindles at just under 5%. 94% of registrants did not make it past the midterm.

How do we explain the 96% stopout¹ rate from course start to course finish? Analyzing completion rates goes hand in hand with understanding student behavior. One MOOC research camp advocates analyzing student usage patterns- resources used, homework responses, forum and Wiki participation - to improve the online learning experience thereby increasing completion rates. Other researchers question the feasibility of analyzing completion rates altogether because the online student body is unpredictable. For example, some students register online because it is free and available with little or no intention of finishing. Some students who leave may lack motivation, or could leave due to personal reasons completely unrelated to MOOCs. As a result, interpreting completion rates is not a straightforward exercise. However, we believe that if we are to fully understand how students learn in MOOCs, we need to better understand why students stopout. Building accurate predictive models is the first step in this undertaking.

Why predict stopout? There are a number of reasons to predict stopout.

- **Interventions**: Stopout prediction in advance allows us to design interventions that would increase engagement, provide motivation and eventually prevent stopout.
- **Identifying intentions**: Certain special cases of stopout prediction allow us to delineate the student intentions in taking the MOOC. For exam-

ple, the cohort for whom we are able to predict stopout accurately based on just their first week behavior could imply that the method and manner in which the course was designed or handled had no effect on the learner's decision to stopout.

Model analysis: Analysis of accurate statistical models that have maximum stopout prediction accuracy can yield insights as to what caused the students to stopout. From this perspective one can even examine the students for whom the predictions were wrong, *that is*, a very accurate and trustworthy model predicted the student would not stopout but the student did stopout. Here the model error could be due to reasons that are unrelated to the course itself.

In a compendium of papers, of which this is first of three, we tackle the challenge of predicting student persistence in MOOCs. Throughout the compendium we focus on the aforementioned course, the Fall 2012 offering of 6.002x: Circuits and Electronics. We believe a three pronged approach which comprehensively analyzes student interaction data, extracts from the data sophisticated predictive indicators and leverages state-of-the-art models will lead to successful predictions. The compendium presents a comprehensive treatment of predicting stopout which produces and considers complex, multi-layered yet interpretive features and fine tuned modeling.

We ask whether it is possible for machine learning algorithms, with only a few weeks of data, to accurately predict persistence. Is it possible to predict, given only the first week of course data, who will complete the last week of the course? How much history (or how many weeks' data) is necessary for accurate prediction one or more week ahead?

1.1. Outline of the compendium

The compendium is organized into the following papers:

- In this paper, we describe the stopout prediction problem, and present a number of discriminatory models we built starting with Logistic regression and moving to Support Vector Machines, Deep Belief networks and decision trees. We also present a summary of which features/variables played a role in gaining accurate predictions.
- In "Towards Feature Engineering at Scale for Data from Massive Open Online Courses" we present how we approached the problem of constructing interpretive features from a time series of click

 $^{^{1}}$ We use stopout as synonymous with dropout and we refer to its opposite as persistence

stream events. We present the list of features we have extracted to create the predictive models (Veeramachaneni et al., 2014b).

• In "Exploring Hidden Markov Models for modeling online learning behavior" we outline a temporal modeling technique called Hidden Markov models and present the results when these models are used to make predictions. We also present a stacked model using both techniques (HMMs and Logisitic regression) and present overview of our findings (Taylor et al., 2014).

Compendium contributions : The most fundamental contribution of this compendium is the design, development and demonstration of a stopout prediction **methodology**, end to end, from raw source data to model analysis. The methodology is painstakingly meticulous about every detail of data preparation, feature engineering, model evaluation and outcome analysis. Our goal with such thoroughness is to advance the state of research into stopout from its current position and document a methodology that is reproducible and scalable. We will next generalize this methodology to a number of additional edX and Coursera courses and report the successes and limitations. In addition, the methodology and software will shortly be released to interested educational researchers.

1.2. Our contributions through this paper

This paper makes the following contributions:

- We successfully predict stopout for the Fall 2012 offering of 6.002x. The major findings of the predictive models are presented in 8.
- We extract 27 sophisticated, interpretive features which combine student usage patterns from different data sources. This included leveraging the collective brain-power of the crowd. These are presented in 3.5.
- We utilize these features to create a series of temporal and non-temporal feature-sets for use in predictive modeling.
- We create over 10,000 comprehensive, predictive models using a variety of state-of-the-art techniques.
- We demonstrate that with only a few weeks of data, machine learning techniques can predict persistence remarkably well. For example we were able to achieve an area under the curve of the receiver operating characteristic of 0.71, given only

one week of data, while predicting student persistence in the last week of the course. Given more data, some of the models reached an AUC of 0.95. We present these and other results in 5.2.

• We build and demonstrate a scalable, distributed, modular and reusable framework to accomplish these steps iteratively.

The rest of the paper is organized as follows. Section 2 presents the details of the data we use, its organization, features/variables we extracted/operationalized for modeling. Section 3 presents the definition of the prediction problem and the different assumptions we make in defining the problem. Section 4 presents the predictive modeling technique - *logistic regression* and the results we achieved for all 91 prediction problems. Section 6 presents the details of how we employed multiple predictive modeling techniques. Section 7 presents the related work both prior to MOOCs and MOOCs. Section 8 presents the research findings relevant to this paper. Section 9 presents our reflection for the entire compendium.

2. Data organization into MOOCdb

As previously mentioned, we focused on the Fall 2012 offering of 6.002x: Circuits and Electronics. edX provided the following raw data from the 6.002x course:

- A dump of click-stream data from learner-browser and edX-server tracking logs in JSON format. For instance, every page visited by every learner was stored as a server-side JSON (JavaScript Object Notation) event.
- Forum posts, edits, comments and replies stored in a MongoDB collection. Note that passive forum data, such as how many views a thread received was not stored here and had to be inferred from the click-stream data.
- Wiki revisions stored in a MongoDB collection. Again, passive views of the Wiki must be inferred from the click-stream data.
- A dump of the MySQL production database containing learner state information. For example, the database contained his/her final answer to a problem, along with its correctness. Note that the history of his submissions must be inferred from the click-stream data.
- An XML file of the course calendar which included information like the release of content and the assignment deadlines.



Figure 1. Multiple data sources received from edX with their corresponding formats

Figure 1 summarizes the raw data received. This data included:

- 154,763 registered learners
- 17.8 million submission events
- 132.3 million navigational events ²
- $\sim 90,000$ forum posts

To analyze this data at scale, as well as write reusable analysis scripts, we first organized the data into a schema designed to capture pertinent information. The resulting database schema, MOOCdb, is designed to capture MOOC data across platforms thereby promoting collaboration among MOOC researchers. MOOCdb utilizes a large series of scripts to pipe the 6.002x raw data into a standardized schema. More about MOOCdb can be found in the MOOCdb Tech report, but the details are outside the scope of this compendium (Veeramachaneni et al., 2014a).

Through the labor intensive process of piping the raw data into a schematized database, we were able to significantly reduce the data size in terms of disk space. The original \sim 70GB of raw data was reduced to a \sim 7GB MOOCdb through schema normalization. The transformation was crucial in order to load the entire database into RAM enabling prompt queries and feature extractions. Figure 2 shows a snapshot of the original JSON transactional data transformed into a normalized schema.

3. Prediction problem definition and assumptions

We made several assumptions to more precisely define the stopout prediction problem and interpret the data. These assumptions include time-slice delineation and defining persistence (stopout) as the event we attempt to predict.

3.1. Time-slice delineation

Temporal prediction of a future event requires us to assemble explanatory variables along a time axis. This axis is subdivided to express the time-varying behavior of variables so they can be used for explanatory purposes. In 6.002x, course content was assigned and due on a weekly basis, where each week corresponded to a module. Owing to the regular modular structure, we decided to define time slices as weekly units. Time slices started the first week in which course content was offered, and ended in the fifteenth week, after the final exam had closed.

3.2. Stopout definition

The next question we had to address was our definition of stopout. We considered defining it by the learner's last interaction in the course, regardless of the nature of the interaction. This is the approach taken by Balakrishnan in his stopout analysis (Balakrishnan & Coetzee, 2013). However, Balakrishnan's definition yields noisy results because it gives equal weight to a passive interaction (viewing a lecture, accessing an assignment, viewing a Wiki etc) as it does to a proactive interaction (submitting a problem, midterm, assignment etc). A learner could stop submitting assignments in the course after week 2, but continue to ac-

 $^{^2 \}rm We$ received more navigational events, but only 132.3 million were well formed enough to be reliably considered for this compendium.



Figure 2. Piping data into MOOCdb



Figure 3. Stopout week distribution

cess the course pages and not be considered stopped out. Instead, we define the stopout point as the time slice (week) a learner fails to submit any further assignments or exercise problems. To illustrate, if a learner submits his/her last assignment in the third module, he/she is considered to have stopped out at week four. A submission (or attempt) is a submission of any problem type (Homework, lab, exam etc.), as defined in MOOCdb. This definition narrows the research to learners who consistently participate in the course by submitting assignments. Using this definition for stopout we extracted the week number when each learner in the cohort stopped out.

Figure 3 shows the distribution of stopout week for all 105,622 learners who ever accessed the course. Of these, 52,683 learners stopped out on week one. These learners never submitted an assignment, and are never considered in the rest of our analysis. Another large learner drop off point is in week 15, the last week of the course. Many of these learners actually finished the course, but did so by submitting their final exam in week 14. This nuance presented itself because learners had a range of time to start the final exam, and this range actually overlapped between weeks 14 and 15. Due to the nature of the final exam time range, we never attempt to predict week 15, and consider week 14 as the final week.

3.3. Lead and Lag

Lead represents how many weeks in advance to predict stopout. We assign the stopout label $(x_1, 0 \text{ for stopout}$ or 1 for persisted) of the lead week as the predictive problem label. Lag represents how many weeks of historical variables will be used to classify. For example, if we use a lead of 5 and a lag of 3, we would take the first 3 weeks of data to predict 5 weeks ahead. Thus, each training data point is a learner's feature values for weeks 1, 2 and 3 as features. The binary stopout value for week 8 becomes the label. Figure 4 shows a diagram of this scenario.

We are careful not to use learners' stopped out week's features as input to our models. In other words, if a learner has stopped out in week 1, 2 or 3, we do not use this learner as a data point. Including stopped out learner data makes the classification problem too easy as the model will learn that a stopped out learner never returns (by our stopout definition).

To illustrate the predictive model's potential application, we will use a realistic scenario. The model user, likely an instructor or platform provider, could use the data from week 1 to week i (current week) to make predictions. The model will predict existing learner stopout during weeks i + 1 to 14. For example, Figure 4 shows one such prediction problem. In this case the user, currently at the end of week 3, is attempting to predict stopout for the 8th week.

Multiple prediction problems Under this definition 91 individual prediction problems exist. For any given week *i* there are 14-i number of prediction problems. Each prediction problem becomes an independent modeling problem which requires a discriminative model. To build discriminative models we utilize a common approach of flattening out the data, that is forming the covariates for the discriminative model by assembling the features from different learner-weeks as separate variables. This process is shown in Figure 7. The example uses data from weeks 1 and 2 (lag of 2) and attempts to predict the stopout for week 13 (lead of 11).

For all of the ensuing modeling and analysis, we treated and reported on each of the cohort datasets independently.

3.4. Partitioning learners into cohorts

Rather than treat all learners uniformly, we decided to build predictive models for different types of learners. With this in mind we divided the learners into cohorts as a rough surrogate variable for their commitment to the course. We chose four cohorts based on the learner's collaborative activity throughout the course. More specifically, we divided learners based on whether or not they participated in the class forum or helped edit the class Wiki pages. The four types of learners are:

- passive collaborator- these learners never actively participated in either the forum or the Wiki. They are named passive because they passively viewed, but did not contribute to, resources.
- wiki contributor- these learners actively participated in the Wiki by generating Wiki content through their edits, but never actively posted in the forum.
- forum contributor- these learners actively posted in the forum, but never actively participated in the class Wiki.
- fully collaborative- these learners actively participated by generating Wiki content and by posting in the forum

From the combined dataset of 52,939 participating learners, we assigned each learner into one of the four types. The chart 5 summarizes the sizes of the cohort datasets.

3.5. Features per learner

We extracted 27 interpretive features on a per-learner basis. These are the features we use to build a model. We describe the process of feature engineering at length in (Veeramachaneni et al., 2014b). In this paper for the sake of brevity, we only list the features and their brief descriptions in the two tables below. For more details about how we came up with these features and how specifically these features were operationalized we refer the readers to (Veeramachaneni et al., 2014b)

4. Logistic Regression

Logistic regression is a commonly used binary predictive model. It calculates a weighted average of a set of variables, submitted as covariates, as an input to the *logit* function. Thus, the input to the *logit* function, z, takes the following form:

$$z = \beta_0 + \beta_1 * x_1 + \beta_2 * x_2 + \dots \beta_m * x_m$$
(1)

	Name	Definition
x_1	stopout	Whether the student has stopped out or not
*x2	total duration	Total time spent on all resources
x_3	number forum posts	Number of forum posts
x_4	number wiki edits	Number of wiki edits
*x5	average length forum post	Average length of forum posts
*x6	number distinct problems submitted	Number of distinct problems attempted
*x7	number submissions	Number of submissions ¹
x_8	number distinct problems correct	Number of distinct correct problems
x_9	average number submissions	Average number of submissions per problem $(x_7 \ / \ x_6)$
x_{10}	observed event duration per correct problem	Ratio of total time spent to number of distinct correct problems (x_2 / x_8). This is the inverse of the percent of problems correct
x_{11}	submissions per correct problem	Ratio of number of problems attempted to number of distinct correct problems $(x_6 \ / \ x_8)$
x_{12}	average time to solve problem	Average time between first and last problem submissions for each problem (average(max(submission.timestamp) - min(submission.timestamp) for each problem in a week))
*x13	observed event variance	Variance of a student's observed event timestamps
x_{14}	number collaborations	Total number of collaborations $(x_3 + x_4)$
x_{15}	max observed event duration	Duration of longest observed event
*x16	total lecture duration	Total time spent on lecture resources
* <i>x</i> ₁₇	total book duration	Total time spent on book resources
*x18	total wiki duration	Total time spent on wiki resources

Table 1. List of self-proposed, self-extracted covariates

 1 In our terminology, a submission corresponds to a problem attempt. In 6.002x, students could submit multiple times to a single problem. We therefore differentiate between problems and submissions.

	Name	Definition
<i>x</i> ₂₀₁	number forum responses	Number of forum responses
*x202	average number of submissions percentile	A student's average number of submissions (feature 9) as compared with other students that week as a percentile
$*x_{203}$	average number of submissions percent	A student's average number of submissions (feature 9) as a percent of the maximum average number of submissions that week
*x204	pset grade	Number of the week's homework problems answered correctly / number of that week's homework problems
x_{205}	pset grade over time	Difference in grade between current pset grade and average of student's past pset grade
*x206	lab grade	Number of the week's lab problems answered correctly $/$ number of that week's lab problems
<i>x</i> ₂₀₇	lab grade over time	Difference in grade between current lab grade and average of student's past lab grade
x ₂₀₈	number submissions correct	Number of correct submisions
<i>x</i> ₂₀₉	correct submissions percent	Percentage of the total submissions that were correct (x_{208} / x_7)
*x210	average predeadline submission time	Average time between a problem submission and problem due date over each submission that week

Table 2. List of crowd-proposed, self-extracted covariates



Figure 4. Diagram of the learners' weeks data used in a lead 5, lag 3 prediction problem



Figure 5. Chart of the relative sizes of our cohorts

Here, β_1 to β_m are the coefficients for the feature values, x_1 to x_m . β_0 is a constant. The *logit* function, given by,

$$y = \frac{1}{1 + e^{-z}}$$
(2)

takes the shape as shown in figure 8. Note that the function's range is between 0 and 1, which is optimal for probability. Also note that it tends to 'smooth out' at extreme input value, as the range is capped.

For a binary classification problem, such as ours, the output of the *logit* function becomes the estimated probability of a positive training example. These fea-

ture weights, or coefficients, are similar to the coefficients in linear regression. The difference is that the output ranges between 0 and 1 due to the logit function, rather than an arbitrary range for linear regression.

4.1. Learning

The objective of training a logistic regression model is to find a set of coefficients well suited to fit the data. For the binary classification problem, as noted before, training involves passing a set of covariates and a corre-



Figure 6. The feature matrix, which captures each feature value for each week. Each student has such a matrix.



Figure 7. Diagram of the flattening process. In this case two weeks of data is used to predict week 13. This prediction problem corresponds to a lead of 11, and a lag of 2.



Figure 8. The logit (aka logistic or sigmoid) function. The logit equation is $y = \frac{1}{1+e^{-x}}$. The range of the function is between 0 and 1.

sponding binary label associated with the covariates. After training a model, the predicted probability, or the output of the *logit* function, should predict higher probabilities for the positive '+1' class examples in the training data and a lower probability for the negative '0' class examples.

There is no closed form solution to find the optimal coefficients to best fit the training data. As a result, training is usually done iteratively through a technique called maximum likelihood estimation (Menard, 2002). First, a random set of coefficients are chosen. At each iteration, an algorithm such as Newton's method is used to find the gradient between what the coefficients predict and what they should predict, and updates the weights accordingly. The process repeats until the change in the coefficients is sufficiently small. This is called convergence. After running this iterative process over all of the training examples, the coefficients represent the final trained model.

4.2. Inference and evaluation

With training in place, the next step is evaluating the classifier's performance. A testing set comprised of untrained covariates and labels evaluates the performance of the model on the test data following the steps below:

- Step 1: The logistic function learned and presented in 2 is applied to each data point and the estimated probability of a positive label y_i is produced for each data point in test set.
- Step 2: A decision rule is applied to determine the class label for each probability estimate y_i . The decision rule is given by:

$$\hat{L}_i = \begin{cases} 1, & \text{if } y_i \ge \lambda \\ 0, & \text{if } y_i < \lambda \end{cases}$$
(3)

Given the estimated labels for each data point \hat{L}_i and the true labels L_i we can calculate the confusion matrix, true positives and false positives and thus obtain an operating point on the ROC curve.

Step 3: By varying the threshold λ in 3 the decision rule above we can evaluate multiple points on the ROC curve. We then evaluate the area under the curve and report that as the performance of the classifier on the test data.

Predictive accuracy heat map To present the results for multiple prediction problems for different weeks simultaneously, as discussed in Section 3.3, we assemble a heat map of a lower right triangular matrix as shown in Figure 9. The number on the x-axis is the week for which predictions are made of that experiment. The y-axis represents the *lag*, or the number of weeks of data used to predict. The color represents the area under the curve for the ROC that the model achieved. Note that as the predicted week increases for a given *lag*, it is harder to predict. Likewise, as we increase the *lag* for a given prediction week, the stopout value becomes easier to predict. This implies that using more historical information enables a better prediction.

4.3. Attractive properties of logistic regression

- It is relatively simple to understand.
- After a model is trained, it provides feature weights, which are useful in assessing the predictive power of features (this will be discussed further in our treatment of the randomized logistic regression model).



Figure 9. Example heatmap for a logistic regression problem. The heatmap shows how the ROC AUC varied as *lag* changed as the target prediction week changed.

• It is fast to run. On a single i-7 core machine, for example, running each of the 91 prediction problems on all 4 cohorts took 25 hours.

5. Predicting stopout with logistic regression

We applied logistic regression to student persistence prediction. We used the 27 interpretive features we described earlier in this paper to form the feature vectors, and maintained the stopout value as the label.

5.1. Experimental setup

To perform logistic regression analysis, we executed the ensuing steps for every lead, lag and cohort combination ³:

- 1. Performed 10 fold cross validation on the training set. As outlined in the evaluation chapter, this involved training the model on 9 folds of the train dataset and testing on the last fold.
- 2. Trained a logistic regression model on the entire train dataset.
- 3. Applied the model to the test dataset by putting each data point through the model then applying the decision rule in 3 and following the steps in 4.2 to determine the AUC under the ROC.
- 4. Evaluating the model using mean cross validation ROC AUC and test set ROC AUC.

³ We used the logistic regression implementation of an open source machine learning library, called scikit-learn. We chose this library because it is well known and tested, fast (the core maximum likelihood estimation algorithm is written in C), with an easy to use python interface. In addition, the scikit-learn library includes an easy interface for cross validation and feature normalization.



Figure 10. Logistic regression results for the passive collaborator cohort.

5.2. Experimental Results

Figures 10 through 13 summarize the AUC of the receiver operating characteristic for all four cohorts over each lead and *lag* combination. Overall, logistic regression predicted dropout with very high accuracy. Some experiments, such as a *lag* of 7, predicting week 8 in the fully collaborative cohort achieved accuracies as high as 0.95, a noteworthy result(Figure 12). Moreover, the entire diagonal of the passive collaborator cohort's heatmap (Figure 10) resulted in an AUC greater than 0.88. This diagonal represents experiments with a lead of one. Thus, we can surmise that the extracted features are highly capable of predicting stopout, especially when the prediction week is fairly near the *lag* week.

Across all experiments, the predictive models of the passive collaborator cohort achieved the highest predictive accuracies. This is because passive collaborator is by far the largest cohort, which resulted in high performing, stable accuracy for all 91 experiments. Conversely, the wiki contributor cohort performed terribly for many experiments. In fact, for some *lag* and predicted week combinations, the model could not even compute an AUC because there were not enough examples to test on. What follows is a deeper explanation of two interesting prediction problems and their results.

Are there early signs of stopout? One interesting prediction problem is trying to predict student persistence into the last week of the course using a single week of data. Practically speaking, this would enable platform providers and instructors to predict which students would finish the course by the end of the first week. Potentially, this would allow instructors to interpret the reason for student stopout as motivational (such as just browsing) rather than course-specific reasons (such as the content becoming too difficult), because the students have not been exposed to much content yet. Furthermore, early-sign stopout prediction could allow courses to target certain types of students for some type of intervention or special content. If our models are successful, the results would imply that our extracted features are capturing a student's persistence far in advance. Remarkably across cohorts. the generated models achieved an AUC of at least 0.64, and reached as high as 0.78 in the case of the wiki contributor cohort.

The wiki contributor AUC of 0.78, or even the passive collaborator of 0.7 suggests it is possible to roughly estimate which students will finish the course. Im-



Figure 11. Logistic regression results for the forum contributor cohort.

plications include the ability to reach out to students likely to stop the course before they become disengaged, or giving a professor a rough indication of how many students to expect each week. If these predictions hold true for other courses, a prediction model could be used to measure the success of course experiments, such as changing course content.

In the case of the wiki contributor cohort, the model performed well for most later predictive weeks given a *lag* of one. This indicates two things. Firstly, wiki contributor students show remarkably strong early signs of persistence. Secondly, given more students, predictive models of the wiki contributor cohort would likely perform well. Owing largely to the small pool size of the wiki contributor cohort, model performance suffered, especially as *lag* increased, because there were not enough students to appropriately train on. However, with a lead of one, the models used more student's data because we included all students who started in the course.

The prediction spike after the midterm Leading up to the midterm (in week 8), making predictions using a *lag* of *i*, where *i* is the current week, yields a fairly consistent AUC. In other words, students who will stopout after the midterm resemble their persistent counterparts up until week 8. However, using *lag* 8 instead of 7, thereby including midterm data, produces an upward prediction spike in all four cohorts.

Perhaps the most striking spike example is in the most consistent cohort, the passive collaborator students. If the model attempts to predict using a only lag 7, it realizes an AUC of 0.75. If the model expands to include midterm week data from week 8 and attempts to predict who will be in the course the next week, it achieves an AUC of 0.91. This is a significant spike. Similarly, the fully collaborative cohort increases AUC significantly from 0.68 in week 7 to 0.81 in week 8.

With the addition of the midterm week data, the model is equipped to make reasonably consistent predictions through the end of the course. In fact, for the two cohorts of significant size, the region including and beyond week 8 achieves the highest AUCs of the entire course. This suggests that the midterm exam is a significant milestone for stopout prediction. It follows that most students who complete the midterm finish the course. For the two smaller cohorts, wiki contributor and fully collaborative, the region beyond week 8 realizes terrible predictive power because too few students remain in the course to accurately train on.



Figure 12. Logistic regression results for the fully collaborative cohort.

Consider what a wiki is (students summarize and reframe their knowledge) and the high level of engagement it reflects (more than forum). Therefore, other technologies that have similar kind of high engagement may have same influence on persistence.

Feature importance We utilized randomized logistic regression methodology to identify the relative weighting of each of the feature. More details about this approach are presented in (Veeramachaneni et al., 2014b). Here we briefly present the results of that experiment through Figure 14. In these four figures higher bar represents higher importance of that feature in predicting stopout across all 91 experiments for that cohort. We summarize the features we found important in the findings section.

6. Multiple classifiers

After successfully modeling the data using logistic regression and Randomized logistic regression, we proceeded to model the data using a number of classifiers via a cloud based machine learning as service framework called Delphi. Delphi is a first-ever shared machine learning service developed by members of ALFA group at CSAIL, MIT (Drevo, 2014)⁴. It is a multi-algorithm, multi-parameter self-optimizing machine learning system that attempts to automatically find and generate the optimal discriminative model/classifier with optimal parameters. A hybrid Bayesian and Multi-armed Bandit optimization system searches through the high dimensional search space of models and parameters. It works in a load balanced fashion to quickly deliver results in the form of ready-to-predict models, confusion matrices, cross validation accuracy, training timings, and average prediction times.

6.1. Experimental setup

In order to run our datasets through Delphi, we performed the following:

1. Chose a few lead, lag combinations to run on Delphi. Since Delphi creates many models, we only chose 3 datasets per cohort. We chose lead and lag combinations which were difficult for logistic regression to predict so we could see if Delphi would perform better. We chose the following combinations: lead of 13, lag of 1; lead of 3, lag of 6; lead

⁴http://delphi.csail.mit.edu/



Figure 13. Logistic regression results for the wiki contributor cohort.

of 6, lag of 4.

- 2. Flattened each cohort's train and test dataset to generate files which could be passed to Delphi. We flattened in the same manner as described in logistic regression section.
- 3. Ran the 12 datasets through Delphi. This gave us 12 models which performed best on a mean cross validation prediction accuracy metric.
- 4. Evaluated these models on the basis of test dataset ROC AUC and cross validation ROC AUC performance.

6.2. Delphi results

The models created by Delphi attained AUCs very similar to those of our logistic regression and HMM models (described in (Taylor et al., 2014). The best algorithm chosen by Delphi varied depending on which lead, lag and cohort combination was chosen. The algorithms included stochastic gradient descent, k nearest neighbors, logistic regression, support vector machines and random forests.

For the two larger cohorts, passive collaborator and forum contributor, Delphi's models used logistic regression, stochastic gradient descent, support vector machines and random forests. For each of the lead and lag combinations, the models' results were within 0.02 of our logisitic regression results. This indicated that the predictive power of these cohorts was not due to the type of model used. Rather, the strong predictive accuracies achieved were due to the interpretive features in the models. As noted in (Veeramachaneni et al., 2014b), varying the features used, such as when using only the self-proposed, self-extracted features rather than the self-proposed, self-extracted features, significantly changed the results. These findings lead us to conclude that focusing on better features provides more leverage in MOOC data science than does fine-tuning models.

For the smaller wiki contributor and fully collaborative cohorts, Delphi's models provided significantly better accuracy. For example, for the wiki contributor cohort, all three lead and lag combinations' models produce AUCs greater than 0.85. The best classifiers used to model these cohorts included k nearest neighbors and stochastic gradient descent. This indicates that for these cohorts, the type of model matters a great deal. We conclude that this is due to the small size of the cohorts. Some classifiers are able to more gracefully



Figure 14. Relative importance of different features across all variants (different lead and lag) of stopout prediction problem. The four plots give the feature importances as found for the four cohorts we described in this paper. Summary: For the passive collaborator cohort, top 5 features that had the most predictive power across multiple stopout predictive problems include average pre deadline submission time, submissions per correct problem, average number of submissions in percent, correct submissions percent, pset grade over time. For the forum contributor cohort, top 5 features that had the most predictive problems include lab grade over time, average pre deadline submission time, average length of forum post, lab grade, average number of submissions in percent. For the fully collaborative cohort, top 5 features that had the most predictive power across multiple stopout predictive problems include lab grade over time, lab grade, pset grade, pset grade over time, average pre deadline submission time. For the wiki contributor cohort, top 5 features that had the most predictive power across multiple stopout predictive problems include lab grade over time, lab grade, average pre deadline submission time. For the wiki contributor cohort, top 5 features that had the most predictive power across multiple stopout predictive problems include lab grade over time, lab grade, average pre deadline submission time, pset grade, average number of submissions include lab grade over time, lab grade, average pre deadline submission time, pset grade, average number of submissions include lab grade over time, lab grade, average pre deadline submission time, pset grade, average number of submissions in percent. For more details about how these relative importances were calculated we refer the user to (Veeramachaneni et al., 2014b).

handle less data. This provides early suggestive evidence that, when a student cohort is relatively small (in relation to number of features), it is important to investigate multiple models to identify the most accurate one.

7. Related work and literature

Dropout prediction and analysis of reasons for dropout have been of great interest to the educational research community in a variety of contexts: e-learning, distance education and online courses offered by community colleges. To understand and gain perspective on what has been done so far, we surveyed a large cohort of relevant literature. Tables 3 present a list of 25 research studies we surveyed that were prior to MOOCs. Table 4 presents the list of 8 concurrent studies that correspond to MOOCs.

We use a set of five axes along to compare research models. For any model, the axes are 1) intended purpose: *predictive* vs. *correlative*, 2) whether *behavioral* and/or *non-behavioral* attributes were employed, 3) use of *longitudinal* and/or *time-invariant* variables and 4) use of *trace data* and/or *survey data*. A subset of these axes are similar to those identified by (Lykourentzou et al., 2009).

Axis 1: Intended Purpose - Predictive vs. correlative By categorizing a model as predictive, we identify it being used *prospectively* to predict the whether or not a student will dropout. Predictive modeling is often the basis of interventions. It can be used while a course is running. In correlative modeling, analysis is performed to correlate one or more variables with completion (or progress to some timepoint). *Retrospectively*, the reasons for dropout are identified. (Diaz, 2002; Tyler-Smith, 2006; Street, 2010) provide an excellent summary of a number of *correlative* studies performed in this domain. Many studies build predictive models to not operationalize the model for actual prediction during a course but to gain insights into which variables and what values of the variables are predictive of dropout. We categorize such approaches as *correlative* as well.

Within the predictive models category, in the literature, there is an abundance of modeling problems set up to use a set of variables recorded over a single historical interval, e.g first 3 weeks of the course, and to predict an event at a single timepoint. For example, using data or surveys collected from the first 4 modules of a course to forecast stopout after the midterm. In some cases, however, when predictive models are built for a number of time points in the course as in (Lykourentzou et al., 2009) the model is not built to

predict ahead.

In contrast, we identify 91 different predictive modeling problems within a single MOOC. We take pains to not include any variable that would arise at or after the time point of our predictions, i.e. beyond the lag interval. We do this so we can understand the impact of different timespans of historical information on predicting at different time intervals forward. In other words, our study is the first to the best of our knowledge to systematically define multiple prediction problems so predictions could be made during every week of the course, each week to the end of the course. (Lykourentzou et al., 2009) provide an excellent summary of studies that fall in *predictive* category.

Finally, we are concerned with the accuracy of predictive model so that it could be used during the course for intervention. As predictions can make two types of errors: *mispredict* stopout or *mispredict* persistence, our use of area under the receiver operating characteristic curve (AUC) as a metric for measuring the efficacy of our models rather than R^2 metric is a testament to the effect. The metric emphasizes the importance of both the errors and we aim at optimizing this metric. To the best of our knowledge this metric has not been used to evaluate the models. Additionally, we provide a *probability of stopout* allowing the user to choose a threshold to make prediction. This allows the intervention designer to choose a trade-off point on the receiver operating characteristic curve.

Axis 2: Behavioral and/or non-behavioral attributes. This categorization identifies whether or not variables that capture learning behavior of student were used in modeling. Examples of a non-behavioral attribute are a student's age, sex or location, occupation, financial status (Parker, 1999; Willging & Johnson, 2009). Second kind of non-behavioral variables are *perceptual* variables, such as those derived from questionnaires, that need to be self reported. Our models do not depend on perceptual variables, neither do they depend on non-behavioral variables such as age, gender and others. While such variables can play a significant role in increasing accuracy of models (especially when predicting far ahead), in a MOOC they may not be available. This is a powerful and significant difference as this allows us to be able to transfer the model without needing personally identifiable information.

Within the use of behavioral data, the most common behavioral variables used are performance related either prior to or during the course. For example, (Lykourentzou et al., 2009) use prior academic performance (education level), other even use high school GPA, college GPA, freshmen year GPA (Morris et al., 2005; Mendez et al., 2008). Some studies compose variables based on project grade and test grades during the course (Lykourentzou et al., 2009). In almost all cases, prior academic performance has been found to be the highest predictor of the student persistence (Mendez et al., 2008; Xenos et al., 2002; Allen & Robbins, 2008).

The second type of behavioral variables are based on students' interaction with the educational resources (online or otherwise) rather than performance on a test or a midterm, or prior academic performance, for example how much time a student spent on lecture videos or whether or not student attended the orientation session. We tackle the challenge of identifying variables that capture students' interactions with the online platform using actual trace analysis (log analysis). We argue that such analysis can enable identification of attributes of the course that could be associated with stopout. For example, a difficult concept, or a rather hard/confusing video.To the best of our knowledge, the exploitation of very detailed trace oriented variables like we derive appears to be not fully exploited.

Axis 3: Time varying vs. time-invariant variables. A time varying variable captures a quantity at different points in time. Many time varying variables are summaries, such as average downloads per day, total minutes watching videos per module. Sometimes they are first processed with scoring, e.g. see the engagement scoring of (Poellhuber et al., 2008), or ranking such as the decile of a participation level each week. In contrast, a time invariant variable is constant over time, e.g. ethnicity. The important choice between these two types is whether dynamics are factored into modeling. For example, we choose time varying variables as a means of capturing behavioral trends.

Most studies that we surveyed capture variables that are summaries over time. Some of these variables by definition are not time dependent such as *attendance at class orientation* (Wojciechowski & Palmer, 2005) and some are usually aggregated for a period in the course (or entire course): *number of emails to the instructor* (Nistor & Neubauer, 2010). In our work we operationalize variables at multiple time points in the course. In this aspect, perhaps the closest approach to ours is (Lykourentzou et al., 2009) where authors form the time varying variables at different points of the course - different sections of the course.

Axis 4: Trace or survey data use Surveys play an important role in analyzing the factors related to persistence.

Surveys allow perceptual data to be self reported and

collected via questionnaires. They permit very specific theory, such as that underlying motivation or engagement to be articulated and used as a reference point for describing a student. They also permit the theory to be tested. Very common among these are studies that focus on collecting information about students *"locus of control"* (Levy, 2007; Parker, 1999; Morris et al., 2005), *satisfaction* (Park & Choi, 2009; Levy, 2007), or *perception of family support* (Park & Choi, 2009), among others.

Many studies struggle to collect this type of the data. To overcome mistakes in manual data entry most surveys are now provided electronically. However, in many cases, not all students submit responses to surveys and questionnaires. Survey data may ask a question which a respondent fails unintentionally to answer accurately (or worse, intentionally).

Trace data is typically logs and counters. It may include participation records. In MOOCs trace data is available at a very fine grained level. Largely, it can be considered as a set of silent, passive observations. However, one needs to build interpretations for the trace data that does not directly capture student states such as *attention*, *motivation*, *satisfaction*.

Student persistence studies in MOOCs In the context of MOOCs, study of factors relating to persistence has been of great interest due to non-completion rates. There have been at least 5 correlative studies which we present in Table 4. These include (Poellhuber et al., 2014; DeBoer et al., 2014; Breslow et al., 2013), for more see Table 4. We categorize these studies as *correlative* as their goal primarily is to identify variable influences on achievement or persistence.

Research studies performed on the same data as ours in this paper show a steady progression in how variables are assembled and progress is made on this data. (Breslow et al., 2013) identify the sources of data in MOOCs and discuss the influences of different factors on persistence and achievement. (DeBoer et al., 2013) identifies the demographic and background information about students that is related to performance. (DeBoer et al., 2014) assembles 20 different variables that capture aggregate student behavior for the entire course. (DeBoer & Breslow, 2014) posits variables on a per week basis and correlates with achievement, thus forming a basis for longitudinal study. Our work, takes a leap forward and forms complex longitudinal variables on a *per student* - *per week basis*. Later, we attribute the success of our predictive models to the formation of the variables.

In (Poellhuber et al., 2014) a logistic regression model with 90% accuracy was (retrospectively) developed for

Paper	Sample size	Category
(Parker, 1999)	100	correlative, behavioral, time-invariant
(Xenos et al., 2002)	1230	correlative, behavioral, time-invariant
(Kotsiantis et al., 2003)	354	predictive, behavioral, time-invariant
(Xenos, 2004)	800	correlative, behavioral, time-invariant
(Zhang et al., 2004)	57549	correlative non-behavioral, time-invariant
(Dupin-Bryant, 2004)	464	correlative, behavioral, time-invariant
(Wojciechowski & Palmer, 2005)	179	correlative, behavioral, time-invariant
(Morris et al., 2005)	211	predictive, behavioral, time-invariant
(Herzog, 2006)	23,475	predictive, behavioral, time-invariant
(Levy, 2007)	133	correlative, non-behavioral, time-invariant
(Holder, 2007)	259	correlative, non-behavioral, time-invariant
(Cocea & Weibelzahl, 2007)	11	predictive, behavioral, time-invariant
(Mendez et al., 2008)	2232	predictive, behavioral, time-invariant
(Hung & Zhang, 2008)	98	predictive, behavioral, time varying
(Moseley & Mead, 2008)	528	predictive, behavioral, time varying
(Juan et al., 2008)	50	correlative, behavioral, time varying
(Boon, 2008)	1050	correlative, behavioral, time-invariant
(Aragon & Johnson, 2008)	305	correlative, non-behavioral, time-invariant
(Allen & Robbins, 2008)	50,000	correlative, behavioral, time-invariant
$(Lykourentzou et al., 2009)^1$	193	predictive, behavioral, time varying
(Willging & Johnson, 2009)	83	predictive, non-behavioral, time-invariant
(Park & Choi, 2009)	147	correlative, non-behavioral, time-invariant
(Nistor & Neubauer, 2010)	209	predictive, behavioral, time varying

Table 3. Related Literature

 1 This article contains a comprehensive overview similar to ours about a variety of studies conducted in dropout prediction over a number of years in the e-learning/online learning context. We follow some of their findings about related work and summarize in this table in addition to a few more studies we found.

Paper	Category	
(DeBoer et al., 2013)	$correlative,\ non-behavioral,\ time-invariant$	
(Yang et al., 2013)	correlative, behavioral, time varying	
(Breslow et al., 2013)	correlative, behavioral, time-invariant	
(DeBoer et al., 2014)	correlative, behavioral, time-invariant	
(DeBoer & Breslow, 2014)	correlative, behavioral, time varying	
(Halawa et al., 2014)	predictive, behavioral, time varying	
(Ramesh et al., 2013)	predictive, behavioral, time varying	
(Balakrishnan & Coetzee, 2013)	predictive, behavioral, time varying	

Table 4. Studies about student persistence in MOOCs

a French language economics course delivered through the Edulib initiative⁵ of HEC Montreal during the spring 2012 semester. We designate this as a correlative model because completion of the final exam was used as an explanatory variable. Univariate models were first constructed to provide information on variable significance. The final logistical regression model integrated significant variables and identified behavioral engagement measures as strongly related to persistence.

Three predictive studies closer to our study here are (Halawa et al., 2014; Balakrishnan & Coetzee, 2013; Ramesh et al., 2013; 2014). All three attempt to predict one week ahead (lead =1)⁶. Among the papers we surveyed (Balakrishnan & Coetzee, 2013; Ramesh et al., 2013) use area under the curve (AUC) as a metric for evaluating the predictive model.

There are three noteworthy accomplishments of our study when compared to these studies above. First, throughout our study we emphasize on variable/feature engineering from the click stream data and thus generate complex features that explain student behavior longitudinally (Veeramachaneni et al., 2014b). We attribute success of our models to these variables (more then the models themselves) as we achieve AUC in the range of 0.88-0.90 for one week ahead for the passive collaborator cohort.

Second we focus on forming features/variables from highly granular, frequently collected *click stream* data which allows us to make predictions for a significantly large portion of students who *do not* participate in forums, and in addition captures learners interaction with resources and assignments. In the course data we worked with, only 8301 out of 52,939 students participated on forums (approximately 15.6%, See Figure 5). We argue that variables derived from learner interactions on forums, as presented in (Ramesh et al., 2013; 2014; Yang et al., 2013) will only be available for a subset of learners.

Third, we split the learner population into four different cohorts and our methodology generates 91 different prediction problems based on different leads and lags and builds models for each of them. These result in 364 different prediction problems requiring modeling.

8. Summary of Research Findings

Our modeling and feature engineering efforts reveal the following: 7 :

- Stopout prediction is a tractable problem. Our models achieved an AUC (receiver operating characteristic area-under-the-curve) as high as 0.95 (and generally ~ 0.88) when predicting one week in advance. Even with more difficult prediction problems, such as predicting student stopout at the end of the course with only one week's data, our models attained AUCs of ~ 0.7 . This suggests that early predictors of stopout exist.
- For almost every prediction week, our models find

⁵http://edulib.hec.ca

 $^{^{6}}$ Except for (Ramesh et al., 2014) which attempts to predict at three different time points in the course

⁷While we refer the reader to (Veeramachaneni et al., 2014b) in the compendium for detailed descriptions of the features we employed for prediction, numbered $x_1 \ldots x_{18}$ and $x_{201} \ldots x_{208}$, we present a summary of our findings.

only the most recent four weeks of data predictive.

- Taking the extra effort to extract complex predictive features that require relative comparison or temporal trends, rather than employing more direct covariates of behavior, or even trying multiple modeling techniques, is the most important contributor to successful stopout prediction. While we constructed many models with a variety of techniques, we found consistent accuracy arising across techniques which was dependent on the features we used. Using more informative features yielded superior accuracy that was consistent across modeling techniques. Very seldom did the modeling technique itself make a difference. A significant exception to this is when the model only has a small number of students (for example, approximately less than 400) to learn from. Some models perform notably better than others on less data.
- A crowd familiar with MOOCs is capable of proposing sophisticated features which are highly predictive. The features brainstormed by our crowd-sourcing efforts were actually more useful than those we thought of independently. Additionally, the crowd is very willing to participate in MOOC research. These observations suggest the education-informed crowd is a realistic source of modeling assistance and more efforts should be made to engage it. See (Veeramachaneni et al., 2014b) for more details.
- Overall, features which incorporate student problem submission engagement are the most predictive of stopout. As our prediction problem defined stopout using problem submissions, this result is not particularly surprising. however submission engagement is an arguably good definition.
- In general, complex, sophisticated features, such the percentile of a student when compared to other students (x_{202} , Table 2), which relates students to peers, and lab grade over time(x_{207} , Table 2), which has a temporal trend, are more predictive than simple features, such a count of submissions (x_7 , Table 1).
- Features involving inter-student collaboration, such as the class forum and Wiki, can be useful in stopout prediction. It is likely that the quality and content of a student's questions or knowledge are more important than strict collaboration frequency. We found that, in particular, the length of forum posts $(x_5, \text{Table 1})$ is predictive, but the

number of posts $(x_3$, Table 1) and number of forum responses $(x_{201}, \text{ Table 2})$ is not. The role of the collaborative mechanism (i.e. Wiki or forum) also appears to be distinctive since, in contrast to forum post length, Wiki edits have almost no predictive power.

9. General reflections for the entire compendium

This extensive project has revealed a combinatorial explosion of MOOC modeling choices. There are a variety of algorithms which one could use, a variety of ways to define a modeling problem and a number of ways to organize data which is fed into modeling. There are also numerous challenges in assembling features while features themselves turn out to be of very high importance. One has work systematically and be thorough in feature definition and model exploration, otherwise one will never know if one has derived the best prediction capability from the data.

To successfully apply the power of data science and machine learning to MOOC analytics, multiple aspects of the process are critical:

Feature engineering One has to be meticulous from the data up – any vague assumptions, quick and dirty data conditioning or preparation will create weak foundations for one's modeling and analyses. Many times painstaking manual labor is required - such as manually matching up *pset* deadlines, etc. We need to be ready to think creatively as you brainstorm and extract features, and be flexible in the ways we assemble them. For example, utilizing the crowd is much richer than just our own expertise.

Machine learning/modeling at scale There are many ways to represent the extracted features datawith or without PCA, temporal and non-temporal, discretized and non discretized. Additionally there are a number of modeling choices - discriminative, generative or mixed models which include many types of classifiers. One has to consider a number of them to enable insights at scale. The alternative results in a much smaller scope with more limited results.

Our ability to build 10,000 models relied on us first building the cloud scale platforms. This is especially true as the machine learning process includes iterations over data definitions, features and cohort definitions. Only through a large scale computational framework are these multiple iterations possible. Throughout our analysis we ran on hundreds of nodes simultaneously, using the DCAP and Delphi frameworks. **Transfer learning prospects** In order to have a lasting impact on MOOC data science, we have to think big! Investing resources only in investigating stopout for one course limits the impacts of the results. With this in mind, we set out to create a reusable, scalable methodology.

From the beginning of the research, we have envisioned creating open source software. This would allow other researchers to apply our methodology to their own MOOC courses. That our software can be used by any other MOOC research, is due to standardization via the shared MOOCdb data schema. Our attention to the scalability of our methods for large data sets also supports wide applicability. The prospect of multiple studies and multi-course studies would be very exciting and most welcome.

Bibliography

- Allen, Jeff and Robbins, Steven B. Prediction of college major persistence based on vocational interests, academic preparation, and first-year academic performance. Research in Higher Education, 49(1):62– 79, 2008.
- Aragon, Steven R and Johnson, Elaine S. Factors influencing completion and noncompletion of community college online courses. The Amer. Jrnl. of Distance Education, 22(3):146-158, 2008.
- Balakrishnan, Girish and Coetzee, Derrick. Predicting student retention in massive open online courses using hidden markov models. In Technical Report No. UCB/EECS-2013-109. EECS, University of California, Berkeley, 2013.
- Boon, Helen J. Risk or resilience? what makes a difference? The Australian Educational Researcher, 35 (1):81-102, 2008.
- Breslow, Lori, Pritchard, David E, DeBoer, Jennifer, Stump, Glenda S, Ho, Andrew D, and Seaton, DT. Studying learning in the worldwide classroom: Research into edxs' first mooc. Research & Practice in Assessment, 8:13-25, 2013.
- Cocea, Mihaela and Weibelzahl, Stephan. Crosssystem validation of engagement prediction from log files. In Creating new learning experiences on a global scale, pp. 14–25. Springer, 2007.
- DeBoer, Jennifer and Breslow, Lori. Tracking progress: predictors of students' weekly achievement during a circuits and electronics mooc. In Proceedings of the first ACM conference on Learning@ scale conference, pp. 169–170. ACM, 2014.
- DeBoer, Jennifer, Ho, Andrew, Stump, Glenda S, Pritchard, David E, Seaton, Daniel, and Breslow, Lori. Bringing student backgrounds online: Mooc user demographics, site usage, and online learning. engineer, 2:0-81, 2013.
- DeBoer, Jennifer, Ho, Andrew D, Stump, Glenda S, and Breslow, Lori. Changing course reconceptualizing educational variables for massive open $_{23}$

online courses. Educational Researcher, pp. 0013189X14523038, 2014.

- Diaz, David P. Online drop rates revisited. The Technology Source, 3, 2002.
- Drevo, Will. Delphi: A Distributed Multi-algorithm, Multi-user, Self Optimizing Machine Learning System. Master's thesis, Massachusetts Institute of Technology, 2014.
- Dupin-Bryant, Pamela A. Pre-entry variables related to retention in online distance education. The American Journal of Distance Education, 18(4):199–206, 2004.
- Halawa, Sherif, Greene, Daniel, and Mitchell, John. Dropout prediction in moocs using learner activity features. In Proceedings of the European MOOC Summit. EMOOCs, 2014.
- Estimating student retention and Herzog, Serge. degree-completion time: Decision trees and neural networks vis-à-vis regression. New Directions for Institutional Research, 2006(131):17–33, 2006.
- Holder, Bruce. An investigation of hope, academics, environment, and motivation as predictors of persistence in higher education online programs. The Internet and higher education, 10(4):245-260, 2007.
- Hung, Jui-Long and Zhang, Ke. Revealing online learning behaviors and activity patterns and making predictions with data mining techniques in online teaching. MERLOT Journal of Online Learning and Teaching, 2008.
- Juan, Angel A, Daradoumis, Thanasis, Faulin, Javier, and Xhafa, Fatos. Developing an information system for monitoring student's activity in online collaborative learning. In Complex, Intelligent and Software Intensive Systems, 2008. CISIS 2008. International Conference on, pp. 270–275. IEEE, 2008.
- Kotsiantis, Sotiris B, Pierrakeas, CJ, and Pintelas, Panayiotis E. Preventing student dropout in distance learning using machine learning techniques. In Knowledge-Based Intelligent Information and Engineering Systems, pp. 267–274. Springer, 2003.

- Levy, Yair. Comparing dropouts and persistence in e-learning courses. *Computers & education*, 48(2): 185–204, 2007.
- Lykourentzou, Ioanna, Giannoukos, Ioannis, Nikolopoulos, Vassilis, Mpardis, George, and Loumos, Vassili. Dropout prediction in e-learning courses through the combination of machine learning techniques. *Computers & Education*, 53(3): 950–965, 2009.
- Menard, Scott. *Applied logistic regression analysis*, volume 106. Sage, 2002.
- Mendez, Guillermo, Buskirk, Trent D, Lohr, Sharon, and Haag, Susans. Factors associated with persistence in science and engineering majors: An exploratory study using classification trees and random forests. *Journal of Engineering Education*, 97 (1):57–70, 2008.
- Morris, Libby V, Wu, Sz-Shyan, and Finnegan, Catherine L. Predicting retention in online general education courses. *The American Journal of Distance Education*, 19(1):23–36, 2005.
- Moseley, Laurence G and Mead, Donna M. Predicting who will drop out of nursing courses: a machine learning exercise. *Nurse education today*, 28(4):469– 475, 2008.
- Nistor, Nicolae and Neubauer, Katrin. From participation to dropout: Quantitative participation patterns in online university courses. *Computers & Education*, 55(2):663–672, 2010.
- Park, Ji-Hye and Choi, Hee Jun. Factors influencing adult learners' decision to drop out or persist in online learning. *Educational Technology & Society*, 12 (4):207–217, 2009.
- Parker, Angie. A study of variables that predict dropout from distance education. International journal of educational technology, 1(2):1–10, 1999.
- Poellhuber, Bruno, Chomienne, Martine, and Karsenti, Thierry. The effect of peer collaboration and collaborative learning on self-efficacy and persistence in a learner-paced continuous intake model. *International Journal of E-Learning & Distance Education*, 22(3):41–62, 2008.
- Poellhuber, Bruno, Roy, Normand, Bouchoucha, Ibtihel, and Anderson, Terry. The relationship between the motivational profiles, engagement profiles and persistence of mooc participants. *MOOC Research Initiative Final Report*, 2014.

- Ramesh, Arti, Goldwasser, Dan, Huang, Bert, Daumé III, Hal, and Getoor, Lise. Modeling learner engagement in moocs using probabilistic soft logic. In NIPS Workshop on Data Driven Education, 2013.
- Ramesh, Arti, Goldwasser, Dan, Huang, Bert, Daume III, Hal, and Getoor, Lise. Learning latent engagement patterns of students in online courses. In Proceedings of the Twenty-Eighth AAAI Conference on Artificial Intelligence. AAAI Press, 2014.
- Street, Hannah D. Factors influencing a learners' decision to drop-out or persist in higher education distance learning. Online Journal of Distance Learning Administration, 13(4), 2010.
- Taylor, Colin, Veeramachaneni, Kalyan, and Una-May, O'Reilly. Hidden markov models for stopout prediction in moocs. *x-arxiv*, 8, 2014.
- Tyler-Smith, Keith. Early attrition among first time elearners: A review of factors that contribute to drop-out, withdrawal and non-completion rates of adult learners undertaking elearning programmes. *Journal of Online learning and Teaching*, 2(2):73– 85, 2006.
- Veeramachaneni, Kalyan, Halawa, Sherif, Dernoncourt, Franck, O'Reilly, Una-May, Taylor, Colin, and Do, Chuong. Moocdb: Developing standards and systems to support mooc data science. arXiv preprint arXiv:1406.2015, 2014a.
- Veeramachaneni, Kalyan, O'Reilly, Una-May, and Taylor, Colin. Towards feature engineering at scale for data from massive open online courses. arXiv preprint arXiv:1407.5238, 2014b.
- Willging, Pedro A and Johnson, Scott D. Factors that influence students' decision to dropout of online courses. *Journal of Asynchronous Learning Net*works, 13(3):115–127, 2009.
- Wojciechowski, Amy and Palmer, Louann Bierlein. Individual student characteristics: Can any be predictors of success in online classes? Online Journal of Distance Learning Administration, 8(2), 2005.
- Xenos, Michalis. Prediction and assessment of student behaviour in open and distance education in computers using bayesian networks. *Computers & Education*, 43(4):345–359, 2004.
- Xenos, Michalis, Pierrakeas, Christos, and Pintelas, Panagiotis. A survey on student dropout rates and dropout causes concerning the students in the course of informatics of the hellenic open university. *Computers & Education*, 39(4):361–377, 2002.

- Yang, Diyi, Sinha, Tanmay, Adamson, David, and Rosé, Carolyn Penstein. Turn on, tune in, drop out: Anticipating student dropouts in massive open online courses. In *Proceedings of the 2013 NIPS Data-Driven Education Workshop*, 2013.
- Zhang, Guili, Anderson, Timothy J, Ohland, Matthew W, and Thorndyke, Brian R. Identifying factors influencing engineering student graduation: A longitudinal and cross-institutional study. *Jour*nal of Engineering Education, 93(4):313–320, 2004.